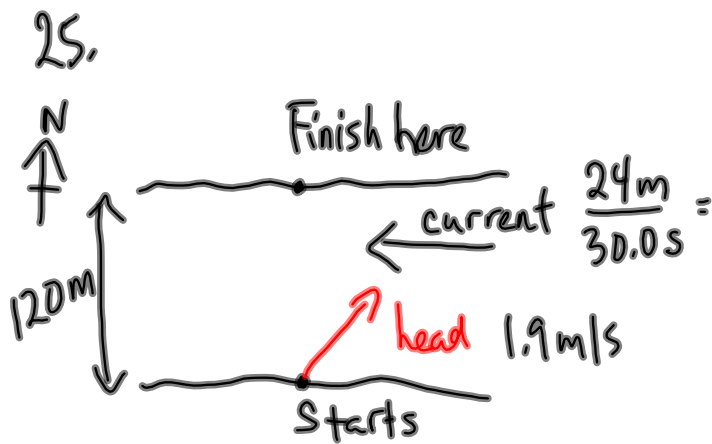
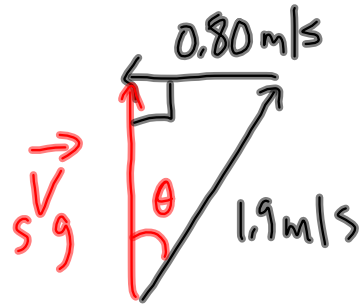


from PP/110



The swimmer should  
head  $[N 25^\circ E]$



To find the heading:

$$\sin \theta = \frac{\text{opp}}{\text{hyp}}$$

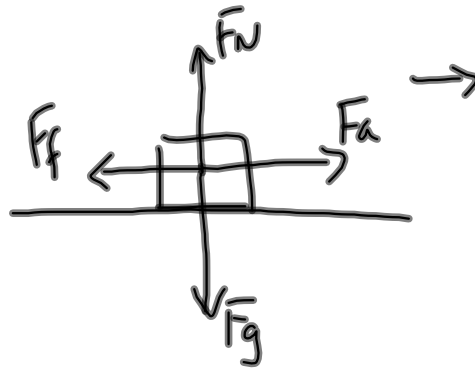
$$\sin \theta = \frac{0.80 \text{ m/s}}{1.9 \text{ m/s}}$$

$$\theta = \sin^{-1} \left( \frac{0.80}{1.90} \right)$$

$$\theta = 25^\circ$$

# Forces + Vectors

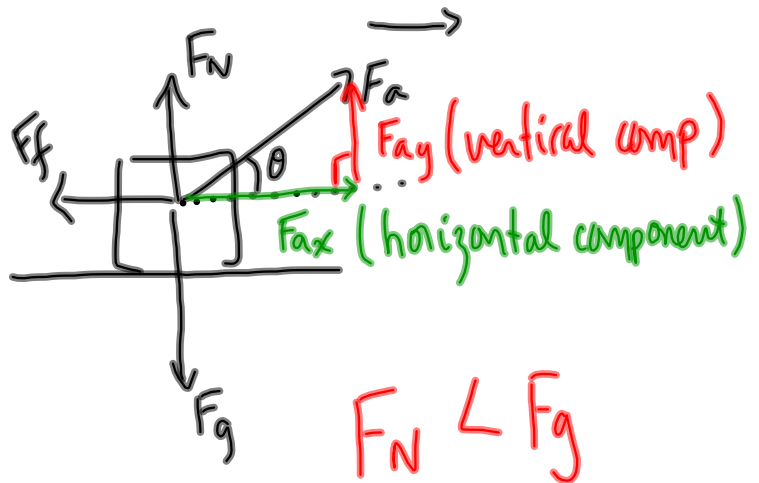
Horizontal Force  
Horizontal Surface



$$F_N = F_g$$

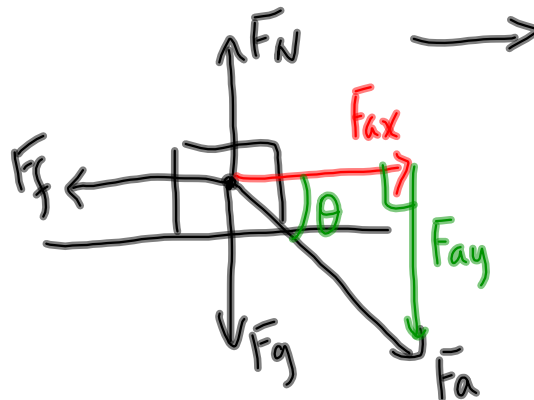
\*  $F_N$  is ALWAYS perpendicular to the surface.

Horizontal surface  
Force is upward at an angle  
i.e. (pulling a wagon)



$$F_N < F_g$$

Horizontal surface  
Downward force at an angle  
(i.e. pushing a cart or a shovel)

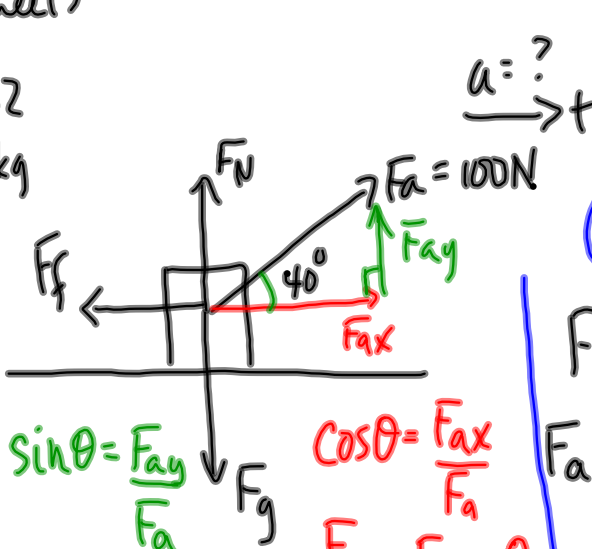


$$F_N > F_g$$

SP (Sheet)

$\mu = 0.32$   
 $m = 20\text{kg}$

side on view



$\sin\theta = \frac{F_{ay}}{F_a}$   
 $F_{ay} = F_a \sin\theta$

$F_{ay} = 100\text{N} \sin 40^\circ$   
 $F_{ay} = 64.3\text{N}$

$\cos\theta = \frac{F_{ax}}{F_a}$   
 $F_{ax} = F_a \cos\theta$

$F_{ax} = (100\text{N}) \cos 40^\circ$   
 $F_{ax} = 76.6\text{N}$

$\vec{F}_{net} = m\vec{a}$

$F_{ax} - F_f = ma$

$F_a \cos\theta - \mu F_N = ma$

$F_a \cos\theta - \mu(F_g - F_{ay}) = ma$

$F_a \cos\theta - \mu mg + \mu F_a \sin\theta = ma$

Solve for a after you sub in values.

$F_f = \mu F_N$

$F_f = 0.32(F_g - F_{ay})$

$F_f = 0.32(196.2 - 64.3\text{N})$

$F_f = 0.32(131.9\text{N})$

$F_f = 42.2\text{N}$

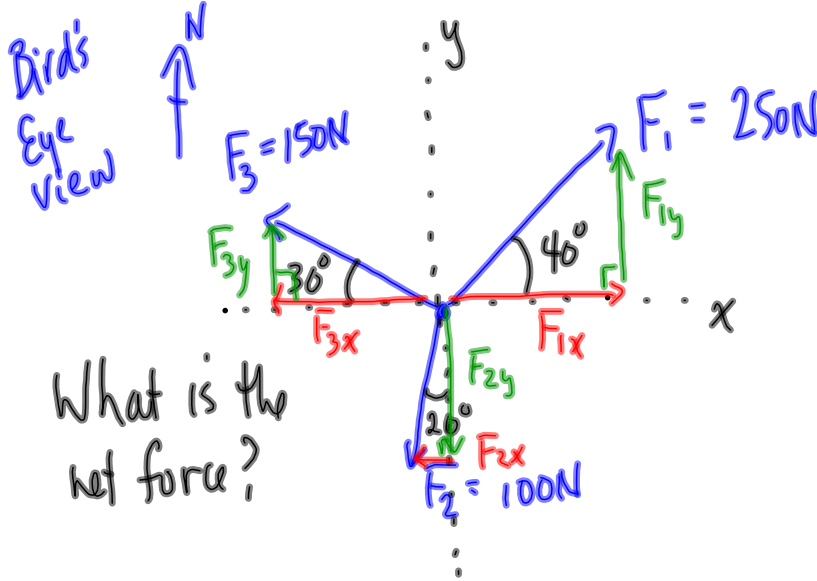
$F_{ax} - F_f = ma$

$76.6\text{N} - 42.2\text{N} = (20\text{kg})a$

$34.4\text{N} = (20\text{kg})a$

$a = 1.7\text{m/s}^2$

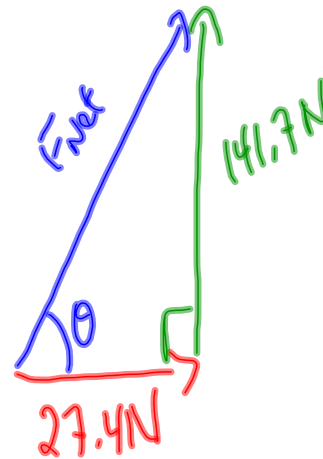
One more example - 3-way Tug-o-war



This is a FBD  
NOT  
a vector addition diagram.

What is the net force?

	x	y
F <sub>1</sub>	250N cos 40° 191.5	250N sin 40° 160.7
F <sub>2</sub>	-100N sin 20° -34.2	-100N cos 20° -94.0N
F <sub>3</sub>	-150N cos 30° -129.9	+150N sin 30° 75N
F <sub>net</sub>	27.4N	141.7N



$$c^2 = a^2 + b^2$$

$$c^2 = (27.4)^2 + (141.7)^2$$

$$c = 144.3 \text{ N}$$

$$\tan \theta = \frac{141.7 \text{ N}}{27.4 \text{ N}}$$

$$\theta = 79.1^\circ$$

$$\vec{F}_{\text{net}} = 144 \text{ N} [E 79^\circ N]$$